

Contour Tracking

Contour Tracking by Stochastic Propagation of
Conditional Density

by Michael Isard and James Blake, in ECCV 1996

Introduction

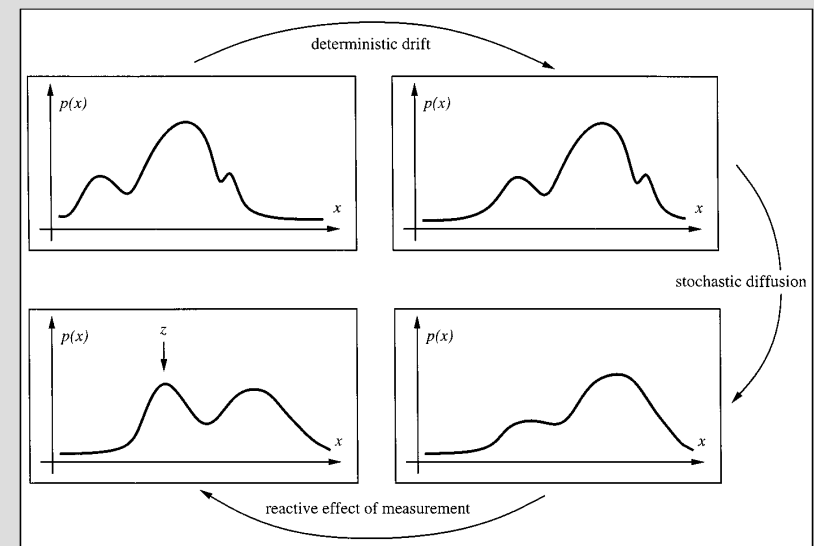
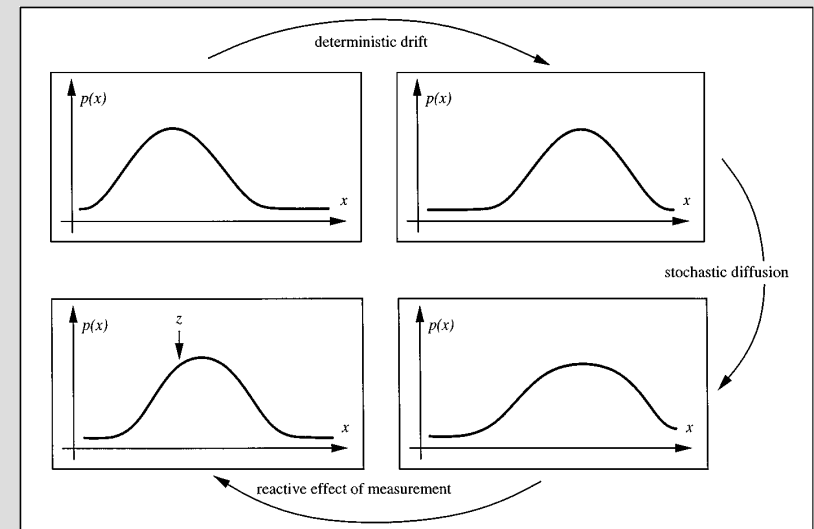
- **Problem:** Track a curve X as it evolves over time given observations Z
- **Particle filter idea:** Stochastically approximate the state posterior $p(X|Z)$ with a set of weighted particles and select $\operatorname{argmax} p(X|Z)$
- **ConDensAtion:** Conditional Density propagAtion

Plan

- Advantage of the Condensation Filter
- Factored Sampling
- Discrete-Time Propagation of State Density
- The Condensation Algorithm
- Shape Modelling
- Examples

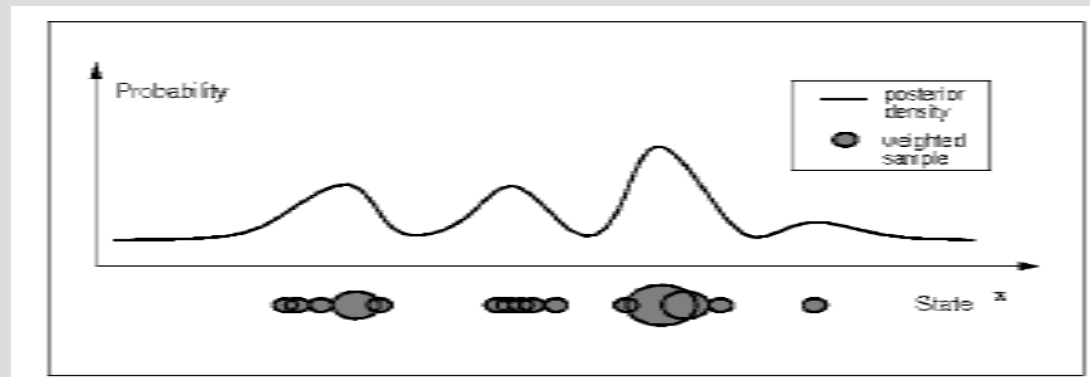
Advantage of the Condensation Filter

- Kalman Filter:
Gaussian densities
- Condensation Filter:
Multi-modal densities



Factored Sampling

- Generate a set of samples that approximates the posterior $p(X|Z)$
- $p(X|Z) = Kp(Z|X)p(X)$
- Sample set $s = \{s^{(1)}, \dots, s^{(N)}\}$ generated from $p(X)$
- Weight for each particle: $\pi^{(i)} = Kp(Z|s^{(i)})$



Discrete-Time Propagation of State Density

- Notation
- Stochastic dynamics
- Measurement
- Propagation

Discrete-Time Propagation of State Density

- Notation

- x_t : state vector, \mathbf{X}_t : history of x_t
- z_t : measurement feature vector, \mathbf{Z}_t : history of z_t
- $p(x)$: prior probability of state vector
- $p(z)$: probability of measuring z
- $p(z|x)$: probability of measuring z given that the state is x
- $p(x|z)$: probability of x given that measurement z has occurred
- Bayes's rule: $p(x|z) = p(z|x)p(x) / p(z)$
- Independence of probabilities: $p(AB) = p(A)p(B)$

Discrete-Time Propagation of State Density

- Stochastic dynamics
 - **Assumption:** temporal Markov chain
 - The new state depends only on the preceding state

$$p(\mathbf{x}_t | \mathbf{X}_{t-1}) = p(\mathbf{x}_t | \mathbf{x}_{t-1})$$

Discrete-Time Propagation of State Density

- Measurement
 - **Assumption:** observations are independent with respect to the dynamical process

$$p(\mathbf{Z}_{t-1}, \mathbf{x}_t | \mathbf{X}_{t-1}) = p(\mathbf{x}_t | \mathbf{X}_{t-1}) p(\mathbf{Z}_{t-1} | \mathbf{X}_{t-1})$$

- **Assumption:** observations are independent mutually

$$p(\mathbf{Z}_{t-1} | \mathbf{X}_{t-1}) = \prod_i p(z_i | \mathbf{x}_i)$$

$$p(\mathbf{Z}_{t-1}, \mathbf{x}_t | \mathbf{X}_{t-1}) = p(\mathbf{x}_t | \mathbf{X}_{t-1}) \prod_i p(z_i | \mathbf{x}_i)$$

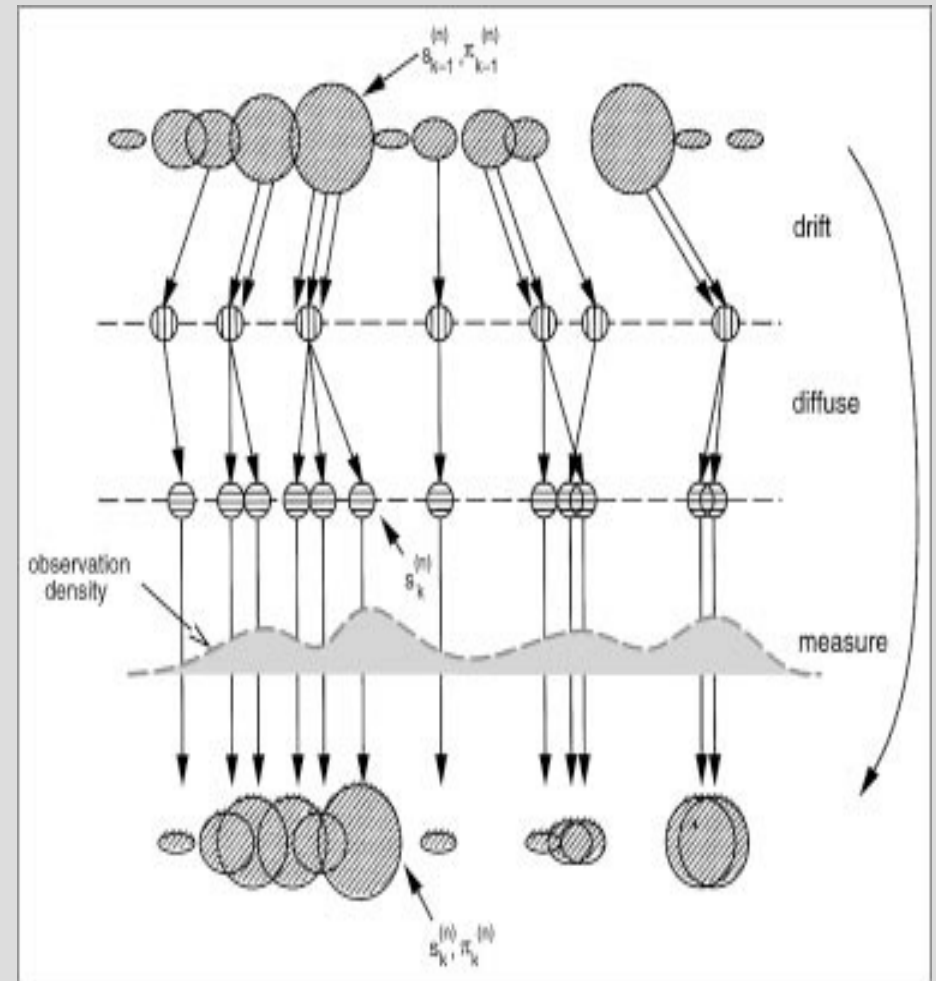
Discrete-Time Propagation of State Density

- Propagation

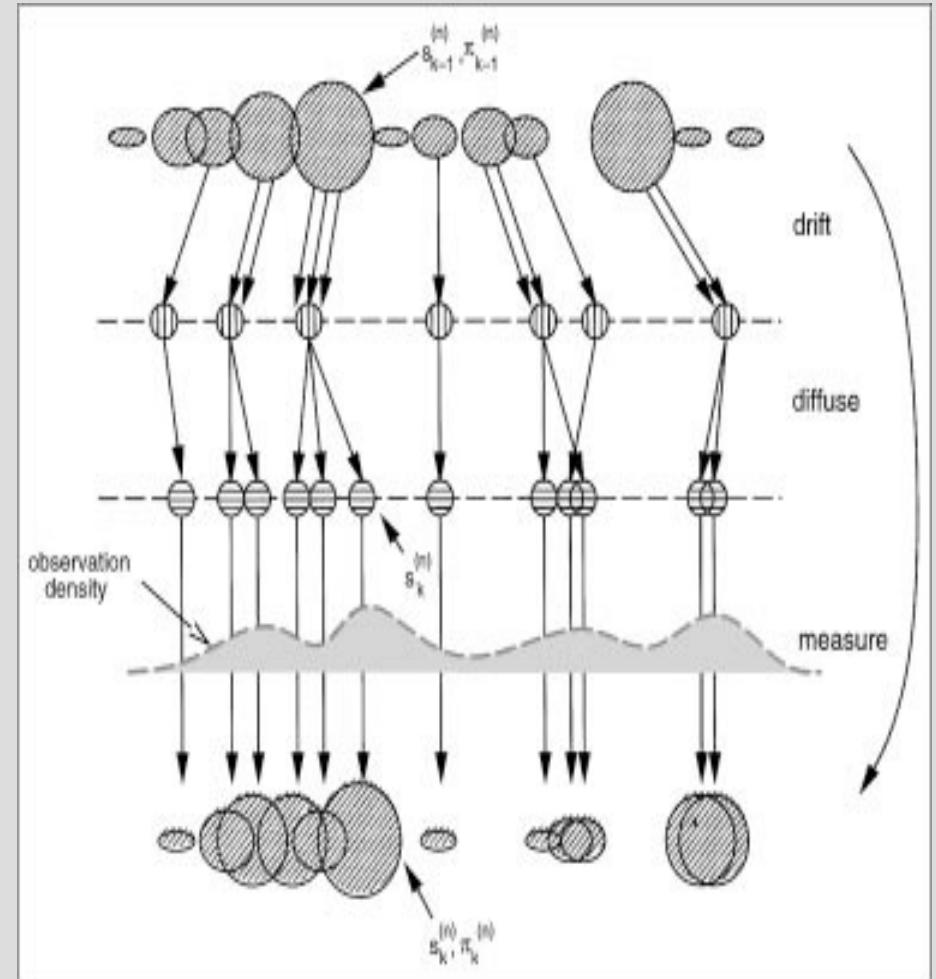
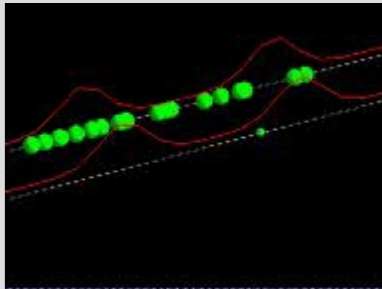
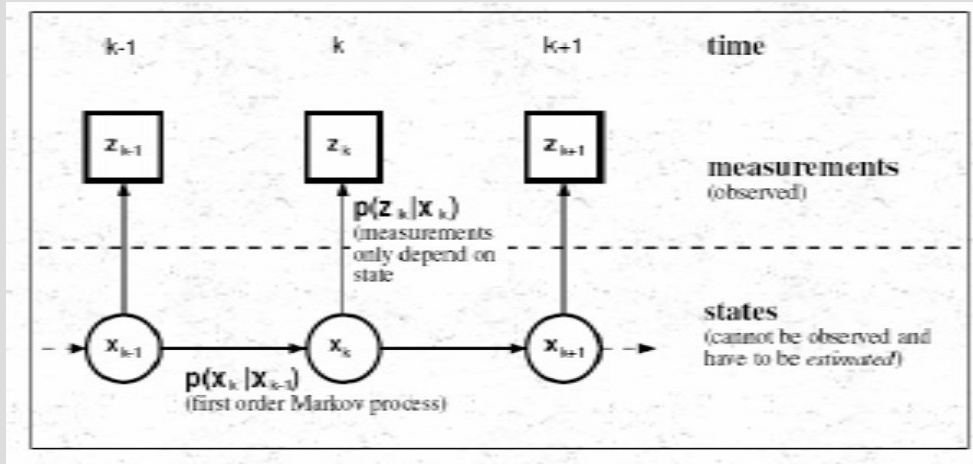
$$p(\mathbf{x}_t | \mathbf{z}_t) = k_t p(\mathbf{z}_t | \mathbf{x}_t) p(\mathbf{x}_t | \mathbf{Z}_{t-1})$$

The Condensation Algorithm

- **1. Select:** N particles from $\{s_{t-1}^{(n)}\}$ (*factored sampling*)
- **2. Predict:** move particles (*drift*) then perturb individually (*diffuse*)
- **3. Measure:** update weight according to image's local appearance to obtain $\{s_t^{(n)}, \pi_t^{(n)}\}$



The Condensation Algorithm



Shape Modelling

- State vector: $\mathbf{x} = (x_c, y_c, \Theta, s)$

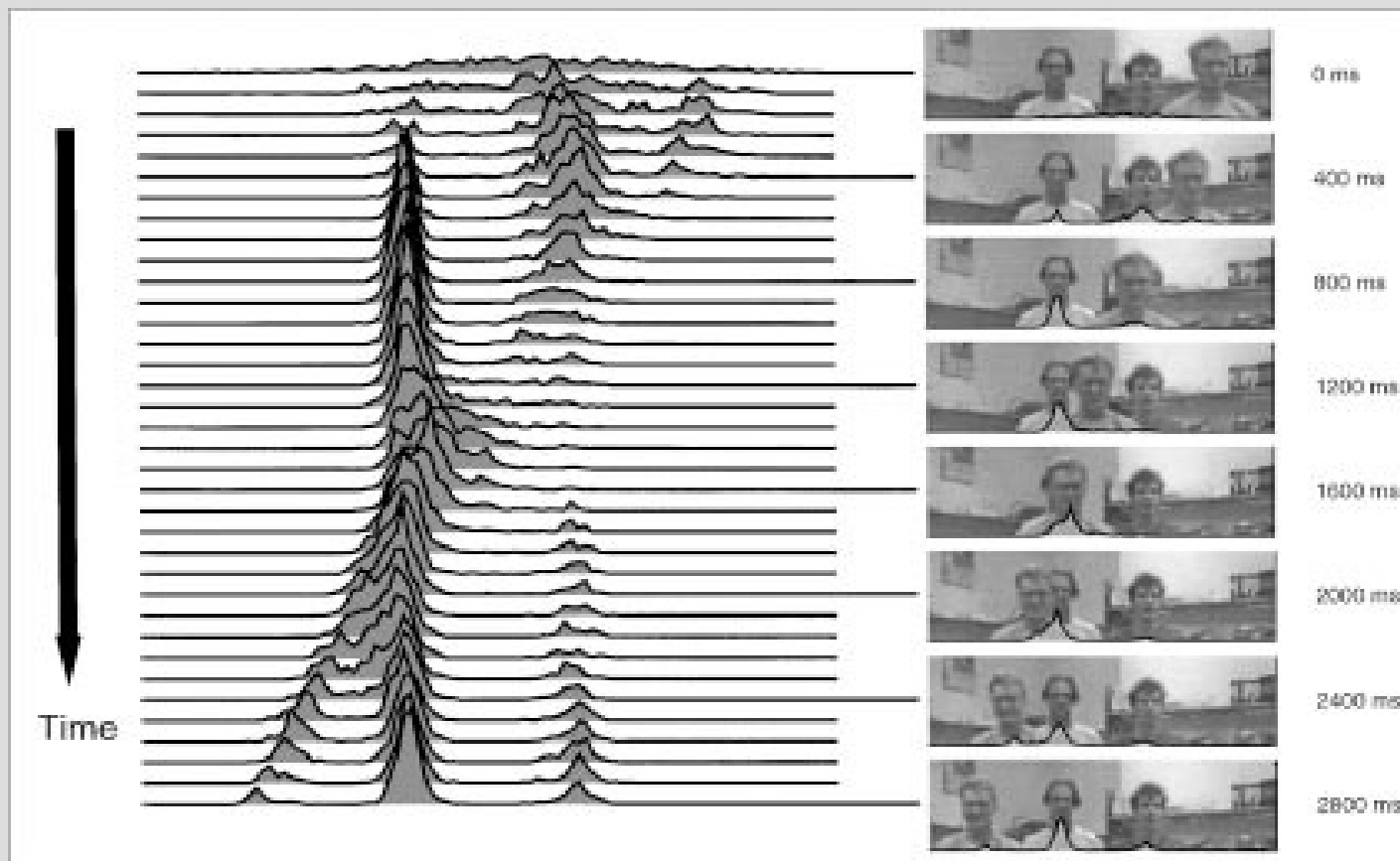
- x_c, y_c : position
- Θ : angle of rotation
- s : scale



- Dynamical model: $\mathbf{x}_t = \mathbf{A}\mathbf{x}_{t-1} + \mathbf{B}\mathbf{w}_{t-1}$

Examples

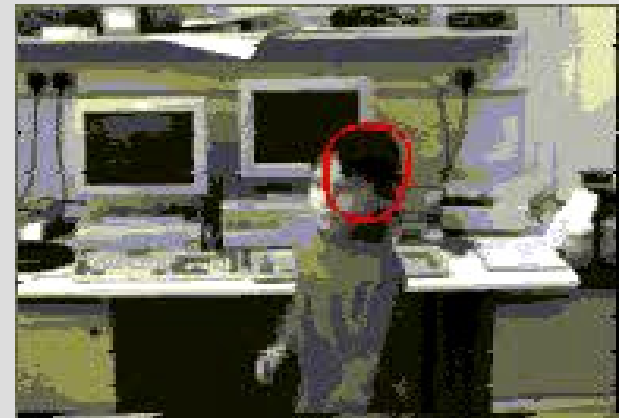
- Tracking a multi modal distribution



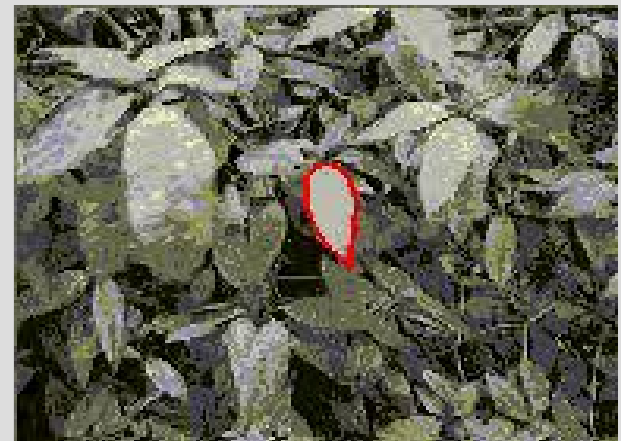
Examples

- Tracking a multi modal distribution

- Tracking rapid motions through clutter



- Tracking a leaf against similar leaves



Examples

- Tracking complex jointed objects

